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To cite this version:

HAL Id: hal-01814491
https://hal.univ-smb.fr/hal-01814491
Submitted on 18 Jun 2018

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Unbiased Electro-Optic Waveguide as a Sensitive Nuclear Magnetic Resonance Sensor

Reina Aydé, Gwenael Gaborit, Jean Dahdah, Lionel Duvillaret, Nadège Courjal, Clement Guyot, Raphaël Sablong, Anne-Laure Perrier, and Olivier Beuf

Abstract—A pigtailed Ti:LiNbO$_3$ waveguide is here associated to a specific nuclear magnetic resonant coil to perform a low invasive magnetic field measurement. The developed device exploits a passive electro-optic transduction between the measured magnetic field and polarization state modulation of a laser probe beam. Because of the use of integrated optics, the coil electromotive force induces a dramatically enhanced electric field, thus leading to sensitivity improvement. A minimum detectable magnetic field lower than 60 fT Hz$^{-1/2}$ is achieved at the resonant frequency of 128 MHz. A dynamic range exceeding 100 dB is experimentally demonstrated.

Index Terms—Electro-optical devices, optical sensors, magnetic field measurement, nuclear magnetic resonance, magnetic resonance imaging.

I. INTRODUCTION

MAGNETIC Resonance Imaging (MRI) constitutes a non invasive technique which provides information related to the anatomy of a living being and allows to diagnosis certain diseases thanks to the analysis of soft tissues. Based on nuclear magnetic resonance (NMR), MRI consists in the study of magnetic modification properties of a nuclei which reflects its interaction with the environment (other nuclei and lattice) [1]. In order to extract this information, it is necessary to modify the magnetization from its equilibrium state, and then to detect its return to this equilibrium state driven by magnetic resonance frequency and different relaxations processes.

Conventionally, an inductive loop is used to characterize the magnetization variations via the induced electromotive force (EMF). The measurement is usually performed with an external coil to image the biological media [2]. However, despite technical MRI improvements, spatial resolution and achievable image quality with external coil are still limited for the examination of deep regions. It has been demonstrated that an endoluminal (internal) coil provides an important increase in local signal to noise ratio (SNR), and enables very high resolution images [3]. Nevertheless, the use of metallic coaxial cable, connecting the coil to the MR system could induce a considerable local specific absorption rate (SAR) especially around this cable [4], [5]. In fact, during a MRI experiment, the radiofrequency (RF) magnetic field is accompanied by an electric (E) field, thus inducing current flow in the metallic cable at the same frequency called common mode. Number of solutions were proposed to reduce this current induced heating [7]–[9]. However, these solutions were not efficient all along the coaxial cable. Optical fibre link can be used to overcome heating problems and to ensure patients safety. In general, to transmit NMR signal from coil to MR system, the direct modulation of laser diode intensity fixed on the probe is applied [10]–[12]. Since direct current supply is required, these methods remain invasive.

Magnetic field characterization involving passive optical system has been already performed [13], [14]. This type of magnetic probe is based on an electro-optic (EO) material associated to a magnetic loop inducing an electric (E)-field proportional to a magnetic field component. This experimental configuration allows to minimize the invasiveness: the probe can be pigtailed, does not need power supply and includes metallic element much shorter than the wavelength of the field to be measured. This kind of sensor has been studied by Suzuki et al. [15] and exploits a magnetic loop doubly loaded with LiNbO$_3$ crystal, acting as the capacitance of the resonator. The realized set-up is dedicated to measure the magnetic field propagating along a stripline, over a wideband of frequencies in the microwave range. The goal is here to develop a resonant EO probe dedicated to RF magnetic field measurement. As our field of interest concerns MRI, the resonant frequency is precisely defined (e.g. 128 MHz corresponding to the proton frequency at 3 T). Moreover, this resonant frequency is lower in MRI system compared to the microwave frequencies, thus inducing a lower electromotive force $e$ applied to the crystal ($e = -\frac{\partial \phi}{\partial t}$ with $\phi$ the magnetic flux). A setup involving a bulk millimetre-sized LiTaO$_3$ crystal...
has been already analysed [16]. The results were in a very good agreement with the theoretical expectations. But using a thinner crystal will lead to a higher internal electric field, thus to an enhanced sensitivity. Moreover, a smaller sensor induces lower disturbances on the external field to be measured. Hence, the purpose of the study is to develop an equivalent set up associated to a matched resonant loop dedicated to magnetic field measurements, where a Ti:LiNbO₃ waveguide replaces a bulk crystal. In the first section, the waveguide transducer performs the E-field induced polarization state modulation (PSM) of a laser beam, and its intrinsic E-field sensitivity is analysed. Subsequently, the EO chip is coupled to the resonant coil to perform magnetic field measurement. The device is optimized in terms of impedance matching. Its linearity response with respect to the magnetic field magnitude is then analysed. The sensitivity is compared to the one obtained with a bulk crystal instead of the optical EO waveguide. The result demonstrates the sensitivity improvement.

II. EO TRANSDUCTION USING AN INTEGRATED LiNbO₃ WAVEGUIDE

The Pockels effect acts in non-centrosymmetric crystals. This EO effect traduces the linear link between the field $\vec{E}$ to be measured and the induced modification of index ellipsoid of the crystal. A detailed study of EO crystal can be found in Ref. [17] and [18]. The developed transducer is based on a LiNbO₃ crystal. The corresponding EO tensor which gives the vectorial dependence of index ellipsoid with the applied electric field $\vec{E}$ is given below:

$$
\begin{pmatrix}
0 & -r_{22} & r_{13} \\
0 & r_{22} & r_{13} \\
0 & 0 & r_{33} \\
0 & r_{51} & 0 \\
-r_{22} & 0 & 0 \\
\end{pmatrix}
$$

(1)

This tensors involves the EO coefficients $r_{ij}$ providing the vectorial behaviour of the EO measurement, i.e. the dependence of the refractive indices $n_i$ to the components $E_j$ of the field vector:

$$
\delta(\frac{1}{n^2})_i = \sum_{j=1}^{3} r_{ij} E_j 
$$

(2)

The optical wave crossing the crystal sees actually two eigen indices $n_+$ and $n_-$. As we here exploit the E-field induced modification of the polarization state of a laser beam, the relevant information is $\delta n(\vec{E}) = \delta(n_+(\vec{E}) - n_-(\vec{E}))$. The E-field induced modifications of the eigen indices are much lower than the intrinsic indices and this latter equation can be rewritten as follow [18]:

$$
\delta n(\vec{E}) = \Delta K \cdot \vec{E}
$$

(3)

The differential sensitivity vector $\Delta K$ gives the direction of electric field component probed by the EO crystal and its modulus leads to the sensitivity of the EO conversion. $\Delta K$ is given by:

$$
\Delta K = \nabla \delta n(E_\Omega)|_{E_\Omega = 0}
$$

(4)

$\Delta K$ depends only on EO crystal properties and on the probe beam direction $\vec{K}$ relatively to the crystal axis. Considering an x-cut wafer of LiNbO₃ with the optical wave propagating along the y-axis of the crystal (see Fig. 1), the sensitivity to the field component $E_z$ takes the value $|\Delta K_{y-prop,E_z}|$. As $r_{ij} \ll n^{-2}$, the modulus of this sensitivity vector becomes:

$$
|\Delta K_{y-prop,E_z}| = \frac{1}{2} (n_z \delta r_{33} - n_x \delta r_{13})
$$

(5)

with $n_x = n_+ = 2.20$ and $n_z = n_- = 2.13$, the eigen indices seen by the optical wave, $r_{13} = 8.6$ pm/V and $r_{33} = 30.8$ pm/V, the EO coefficients involved in the $E_z$ component probing. The field $|E_z|$ to be probed is induced by the EMF $e = V_z$, corresponding to the potential difference applied to the gold electrodes. Hence, the separating distance $d$, between the electrodes is here of major importance in order to reach very high sensitivity: while electrodes placed on sides of a bulk crystal are usually separated by a distance lying in the millimetre range, the optical waveguide transverse dimensions are approximately 10 µm (for the optical wavelength $\lambda_{opt} = 1550$ nm), leading potentially to a significant enhancement of the induced field ($E_z \propto \sqrt{V}$), so that to the response of the sensor.

The transverse transducer consists in a Ti-diffused LiNbO₃ waveguide (length $L_y = 6$ mm, in agreement with the NMR coil dimensions) confined in between two coplanar electrodes lying in the yz plane and separated by a distance $d = 18$ µm. This distance ensures a sensitivity enhancement together with an homogeneous E-field (in modulus and direction) seen by the optical beam. Moreover this configuration induces a capacitance which can be compensated (see section III).

A schematic of the EO chip is proposed in Fig.1. A FDTD simulation (Quickfield®) has been performed in order to assess the induced electric field $E_z$ between electrodes, in the optical waveguide location. The result is given in Fig.2.

This E-field $E_z$ will lead to a dephasing between the two allowed polarization state inside the EO crystal and is finally
The PSM is finally optically treated with a quarter wave plate to compensate the static birefringence of the crystal, and with a polarizer to convert the PSM into a modulation of optical power. An amplified high speed photodiode ensures the last conversion to an electrical signal.

The response of the realized waveguide EO transducer has been characterized. For that purpose, a synthesizer feeds the electrodes at the frequency of interest \( f = 128 \) MHz and the EO signal \( P_{EO,dBm} \) is recorded with a spectrum analyser as a function of the delivered power \( P_{in,dBm} \). Fig.3 illustrates the obtained result. The experimental characterization can be fitted with the equation involving the delivered power itself as well as the noise contribution:

\[
P_{EO,dBm} = 10 \log_{10}(10^{-85 A/W} + 10^{\alpha P_{in,dBm}} + \beta)}
\]

The coefficients \( \alpha \) and \( \beta \) are the linearity factor and the conversion efficiency, respectively. This latter one is determined by the EO conversion itself \( \Delta \varphi \), but also to the optical power carrying the modulation \( 1 \) mW and to the photodiode responsivity \( 0.85 \) A/W.

The measurements dynamic range exceeds 100 dB. The minimum detectable field \( E_{min} \) is obtained equalizing the linear behaviour of the chip and the Johnson-Nyquist noise floor of the spectrum analyser and of the photodiode electronics \( (Noise_{dBm} = -105 \) dBm). \( E_{min} \) is here lower than \( 10 \) mV.m\(^{-1}\).Hz\(^{-1/2}\). This latter value corresponds to a root mean square (RMS) voltage \( V_z < 0.3 \) \( \mu \)V. Moreover the linear slope of the measurement is \( \alpha = 0.98 \) and the standard deviation of the error distribution is about 0.5 dB (see inset of Fig.3). The conversion efficiency between \( P_{in} \) and \( P_{EO} \) is \( \beta = -3 \) dB.

III. THE ELECTRO-OPTIC RESONANT COIL

Based on previous work [19], a reference rectangular coil was built with an external width set to 5.1 mm and a length 1268 IEEE PHOTONICS TECHNOLOGY LETTERS, VOL. 26, NO. 12, JUNE 15, 2014
The nominal resonance, its intrinsic and non-negligible capacitance. In order to retrieve shifts the sensor resonance toward lower frequencies, due to additional amplification of the signal. Finally, the equation 8 is demonstrated and reaches more than 57 dB, without any noise.

Fig. 6. EO NMR coil response as a function of the applied magnetic field. ($f = 128$ MHz, RBW = 30 Hz). Black dots and gray dashed line corresponds to measurement data and fitting curve respectively. Inset illustrates the deviation between measurement data and theoretical fitting curve. Additional gray curve is linked to a previous measurement obtained with a bulk LiTaO$_3$ crystal 4 mm-thick. Dot-dashed line indicates the intrinsic resonant coil (galvanic linked) response.

(gray line). The curve shows that the addition of the EO chip shifts the sensor resonance toward lower frequencies, due to its intrinsic and non-negligible capacitance. In order to retrieve the nominal resonance, $C_i$ has been adjusted to 35.2 pF to compensate capacitance value of the EO chip and inductance of bonding connection. Measurement of $P_{EO}$ in this case is presented with the black line of Fig. 5.

The linearity response of the realized EO coil has been investigated as a function of the applied magnetic field. The result is presented in Fig. 6. Once again, the linearity measurement exhibits a dynamic range greater than 100 dB. The fitting curve gives the magnetic field $B$ response and is written:

$$P_{EO}(dBm) = 10\log_{10} \left( 10^{\frac{N_{core}(dBm)}{10}} + 10^{3}\alpha_{EOcoil} B^2 \right)$$  

(8)

The coefficient $\alpha_{EOcoil}$ is the link between the EO resonant coil signal and the magnetic field to be probed. $\alpha_{EOcoil}$ takes here a value of $1.27 \times 10^{11}$ W.T$^{-2}$, which corresponds to a linear coefficient of $R_{EOcoil} = 2.5 \times 10^6$ V.T$^{-1}$, $R = 50$ Ω being the resistive load. This measurement allows to determine the minimum detectable magnetic field $B_{min} = 0.3$ pT in the 30 Hz resolution bandwidth (RBW) leading to $B_{min} = 56$ fT Hz$^{-1/2}$. Furthermore, this measurement is compared to a similar setup involving a bulk LiTaO$_3$ crystal (4 mm thick) [16]. An increase in sensitivity is demonstrated and reaches more than 57 dB, without any additional amplification of the signal. Finally, the equation 8 can be applied for the magnetic field response of the intrinsic NMR coil in its nominal use (galvanic linked and 50 Ω loaded, see dotdashed line on Fig. 6). It allows to determine $\alpha_{coil} = 1.23 \times 10^{10}$ W.T$^{-2}$, ten times lower than the achieved value of $\alpha_{EOcoil}$ (with the fibre link and the EO conversion).

IV. CONCLUSION

An EO waveguide has been coupled to a resonant coil to design a pigtailed deported and sensitive magnetic field sensor. The use of integrated optics allows to apply the coil EMF on a weak separating distance leading to the enhancement of the field strength seen by the laser probe beam. The passive EO chip exhibits a linear response over a dynamic range exceeding 100 dB. A magnetic field as low as 300 fT remains detectable at the resonant frequency $f = 128$ MHz. The sensor response is increased by more than 50 dB compared to the use of a bulk crystal and by 10 dB compared to the galvanic linked NMR coil. Finally, the millimetre size and the composition of the device are fully suitable for further developments concerning low-invasive and endoluminal MR coils.

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