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Potentialities of an Electro-Optic Crystal Fed by Nuclear Magnetic Resonant Coil for Remote and Low-Invasive Magnetic Field Characterization

Reina Aydé, Gwenaël Gaborit, Pierre Jarrige, Lionel Duvillaret, Raphaël Sablong, Anne-Laure Perrier, and Olivier Beuf

Abstract—In this paper, we demonstrate the use of a LiTaO₃ crystal associated with a typical nuclear magnetic resonant loop coil to perform an optically remote radio frequency magnetic-field characterization. The whole transduction scheme is theoretically and experimentally studied. The measurement dynamics reaches 60 dB. The minimum detectable magnetic field is lower than 1 nT, which corresponds to an induced inner crystal electric field as low as 30 mV/m. To evaluate the spatial potentialities of the sensor, a 1-D mapping of the field along an asymmetric butterfly-shaped loop coil is performed. The result is in good agreement with finite-difference time-domain simulations and demonstrates the vectorial behavior of the sensor device.

Index Terms—Electro-optics, magnetic field sensor, magnetic resonance imaging, nuclear magnetic resonance.

I. INTRODUCTION

MAGNETIC resonance imaging (MRI) is based on a spatial characterization of the nuclear magnetization. Recording the variation of the nuclear magnetization is often realized with a MRI external surface coil. However, spatial resolution and image quality achievable with external surface coils are limited in the case of thin internal organs, e.g. bowel. On the other hand, the use of an endoluminal MRI coil located close to the area of interest could provide both high contrast to noise ratio (CNR) and high spatial resolution images leading, in turn, to a good evaluation of biological diseases [1], [2].

Since metallic coaxial cables are mainly used with endoluminal coils, also located within the MRI transmit RF coil, heating phenomena may occur inside biological media [3]. Optical fibre link can be used to overcome heating problem, thus ensuring patients safety [4], [5]. Direct modulation of a laser diode remains invasive because its biasing requires a DC power supply [4]. Furthermore, the achieved realizations including active devices may also be disturbed by the static magnetic field [4], [6], [7].

Magnetic field characterization involving passive optical system has already been performed [8]–[11]. This type of magnetic probe is based on an Electro-Optic (EO) material associated to a magnetic loop inducing an electric (E)-field proportional to a magnetic field component. This experimental configuration allows to minimize the invasiveness: the probe can be pigtailed, does not need power supply and includes metallic element much shorter than the wavelength of the field to be measured. This kind of sensor has been studied by Suzuki et al. [8] and exploits a magnetic loop double loaded with LiNbO₃ crystal, acting as the capacitance of the resonant equivalent circuit. The realized set-up is dedicated to measure the magnetic field associated to a microwave electromagnetic field propagated along a stripline. We here propose a similar configuration, dedicated to MRI based RF magnetic field measurement. Nevertheless, as our field of interest concerns proton MRI, the resonant frequency is precisely defined (e.g. 127 MHz at 3 T). Moreover, this resonant frequency is lower in MRI system compared to the microwave frequency probed by Suzuki et al., thus inducing a lower electromotive force $e = \frac{d\phi}{dt}$ applied to the crystal. $\phi$ represents the magnetic flux. The loop coil is designed to be intrinsically resonant at 127 MHz and the crystal capacitance is kept very low to keep the same frequency response. In the first section of the paper, the crystal orientation and the measurement set-up are studied and optimized in order to maximize the sensitivity, the linearity and the measurement dynamics. Then, the experimental set-up used for the characterization of the EO magnetic probe is depicted. The response intensity of the probe is measured versus applied magnetic field amplitude. Finally, last section is dedicated to 1D magnetic field mapping of a butterfly-shaped loop RF coil.
II. THEORETICAL BACKGROUND AND MEASUREMENT SET-UP

A. Endoluminal Coil Design

Based on the previous study by Armenean et al. [1], we choose the parameter of the coil as those providing the best signal-to-noise ratio (SNR) for MRI together with suitable dimensions for endoluminal investigations. Hence, the coil has a rectangular shape with an external width set to 5.1 mm, respecting medical constraints, and a length set to 47 mm providing good image penetration depth and exploration length. A 35 μm-thick copper coil is engraved on an insulating substrate FR4 (εr = 4 and thickness T = 0.8 mm). A conductor width of 0.8 mm is defined to minimize ohmic losses then providing the best SNR images. The coil is tuned to a frequency of 127 MHz and is matched at 50 Ω, using capacitors of 282 pF and 39 pF on distal and proximal part of the coil, respectively. A schematic and a picture of the endoluminal coil are presented in figure 1.

The characterization of the coil was performed thanks to a vector network analyzer and the magnitude of S11 reflection coefficient is given in figure 2. The resonant frequency is 126.9 MHz and its bandwidth is 3.5 MHz at −3 dB.

The extracted parameters of the RLC series equivalent circuit are R = 0.85 Ω, L = 46 × 10^{-9} H and C = 34.2 × 10^{-12} F. These values are very close to the expected ones, obtained thanks to method of moments simulations.

B. Electro-Optic Transducer

The Pockels effect appears as an E-field induced modification of the eigen refractive indices in non-centrosymetric crystals. The developed transducer is based on an x-cut LiTaO3 crystal. An exhaustive analysis of the properties of EO crystals is described by Duvillaret et al. [12]. The EO tensor, which gives the vectorial dependence of the index ellipsoid with the E-field is the following one:

\[
\begin{pmatrix}
0 & -r_{22} & r_{13} \\
0 & r_{22} & r_{13} \\
0 & 0 & r_{33} \\
r_{51} & 0 & 0 \\
r_{51} & 0 & 0 \\
r_{22} & 0 & 0
\end{pmatrix}
\]

This latter one leads to the refractive index ellipsoid equation (eq. 1):

\[
x^2 \left( \frac{1}{n_x^2} - E_x r_{22} + E_z r_{13} \right) + y^2 \left( \frac{1}{n_y^2} + E_x r_{22} + E_z r_{13} \right) + z^2 \left( \frac{1}{n_z^2} + E_y r_{33} \right) + 2 E_x r_{51} y z + 2 E_x r_{51} x z - 2 E_x r_{22} x y.
\]

A figure of merit can be calculated for this crystal [12]. As the crystal acts as a polarization state modulator, the relevant property is the E-field induced birefringence \( \delta n = n_+ (\vec{E}) - n_- (\vec{E}) \). The EO figure of merit is depicted by the sensitivity vector \( \vec{\Delta K} \), linked to the relative variation of refractive indices induced by the applied E field. This sensitivity vector is defined by:

\[
\vec{\Delta K} = \vec{\nabla} \delta n(\vec{E})|_{\vec{E}=0}.
\]

Its modulus gives the sensitivity of the EO crystal to the applied E field while its direction leads to the unique E-field component that will be probed. These properties are summarized by the following expression:

\[
\delta n(\vec{E}) \equiv \delta n(\vec{E} = \vec{0}) + \vec{\Delta K} \cdot \vec{E}.
\]

A three-dimensional representation of \( \vec{\Delta K} \) is given in figure 3.

We here consider an x-cut LiTaO3, leading to a high sensitivity together with a transverse E-field probing (see Figure 3: Λ = 90°). For an applied E field along z axis, we get:

\[
|\vec{\Delta K}_{x=\text{cut},E_z}| = \frac{1}{2} \begin{pmatrix} n_z^3 r_{33} - n_y^3 r_{13} \end{pmatrix}.
\]

The theoretical value of \( |\vec{\Delta K}_{x=\text{cut},E_z}| \) at the wavelength of 1550 nm is 120 pm/V assuming \( n_z = 2.116, n_y = 2.117, r_{13} = 7.5 \text{ pm/V}, \) and \( r_{33} = 33 \text{ pm/V} \).

The E-field induced dephasing between the two allowed polarization state inside the EO crystal writes:

\[
\Delta \phi = \frac{2\pi}{\lambda_{\text{opt}}} |\vec{\Delta K}_{x=\text{cut},E_z}|. E_z L_x.
\]

\( \lambda_{\text{opt}} \) being the wavelength of the probing optical beam and \( L_x \), the length of the crystal.
LiTaO₃: $\Delta K^2$

Fig. 3. LiTaO₃ figure of merit for $\Delta K$. $|\Delta K|$ is determined by the distance to the origin. Color: angle $\Lambda$ corresponding to the sensitivity axis orientation between $\Delta K$ and the optical wave-vector $\vec{K}$. Scale at the bottom left. Projections onto the reference planes at the right side. The unit of $|\vec{K}|$ is pm/V⁻¹.

C. Measurement Set-Up

The magnetic field source is constituted of a single wide band loop with a diameter $\varnothing = 10$ cm to provide an homogeneous field onto the endoluminal coil surface. As the dimension of the transmit coil is much shorter than the wavelength of the signal at 127 MHz, $B_x$ is thus directly linked to the input power $P_{in, dBm}$ of the emission coil, via Biot and Savart equation:

$$B_x = \frac{\mu_0 I_c}{2} \frac{a^2}{(a^2 + x^2)^{3/2}}$$  \hspace{1cm} (6)

with $a$ being the radius of the emitting loop and where $I_c = \sqrt{\frac{P_{in, dBm} - 30}{R_{em}}}$. $R_{em}$ is the resistive load of the emission loop and takes a value of 8 $\Omega$ at 127 MHz.

This emission coil is fed by a function generator providing a CW signal at the frequency of 127 MHz. The electrical power $P_{in}$ varies from 14 dBm down to $-60$ dBm thanks to additional RF attenuators. The induced magnetic field at the center of the loop ranges from 700 nT down to 140 pT.

The endoluminal coil is positioned in front of the emission coil and probe the field $B_x$ (see Fig. 4). It induces a $rms$ electromotive force $e$ onto the $z$-axis of the crystal thanks to copper deposited parallel electrodes, thus applying an electric field $E_z = \frac{e}{h_z}$, $h_z$ being the separation distance between electrodes.

The electric field induces a modulation of the laser polarization state. This latter one can be written as a function of the input power $P_{in, dBm}$ feeding the transmit coil and of the coupling factor $\kappa_{ant}$ between the transmit loop and the endoluminal coil:

$$E_z(P_{in, dBm}) = \sqrt{\frac{R_{load} 10^{P_{in, dBm}/10} \kappa_{ant} \cdot \Delta \varphi}{h_z}}$$  \hspace{1cm} (7)

with $R_{load} = 50$ $\Omega$ being the resistive load of the endoluminal coil.

For $x = 0$ (at the center of the loop), equations 7 and 6 lead to the link between $E_z$ and $B_x$:

$$E_z(B_x) = \frac{2a10^{50\kappa_{ant} \cdot \Delta \varphi}}{h_z \mu_0} R_{load} B_x.$$  \hspace{1cm} (8)

The optical source is a low noise DFB laser ($\lambda = 1.55 \mu m$ and Relative Intensity Noise $RIN = -160$ dBc/Hz⁻¹) servo-controlled in temperature and in optical power ($P_{opt} = 50$ mW). A half waveplate orients the impinging linear polarization with an angle of 45° relatively to the crystal axes to maximize the conversion between the field to be measured and the polarization state modulation of the laser probe beam. The modulated polarization state is then analysed thanks to a quarter waveplate, compensating the intrinsic static birefringence of the crystal. A polarizer converts the relative dephasing $\Delta \varphi$ into a modulation of optical power $P_{opt} = \frac{1}{2} \Delta \varphi P_{opt}$. This optical modulation is finally converted into an electrical signal using an amplified ($G = 37.3$ dB) pigtailed high-speed photodiode (sensitivity $\eta = 0.85$ A/W, loading resistance $R_{ph} = 50$ $\Omega$). The mean optical power received by the photodiode after polarization treatment and fibre coupling is $P_{opt} = 14.4$ mW. This latter signal carries the modulation and is then recorded using a spectrum analyzer.

III. EXPERIMENTAL CHARACTERIZATION

The analysis of the signals at different transduction stages, from the emission to the optoelectronic output is firstly investigated. Figure 5 illustrates the spectrum of the input signal feeding the transmit coil, the endoluminal coil received signal and the EO converted signal. The resolution bandwidth (RBW) of the measurement is 30 Hz. It can be noticed on figure 5(a), that the noise floor increases by 40 dB after the first stage of transduction. This is due to internal attenuation of the spectrum analyser that automatically sets for high level signals. Finally, the conversion factors are $\kappa_{ant} = -22 \pm 0.3$ dB and...
\( \kappa_{EO} = -34.7 \pm 0.3 \text{ dB} \) for the detection coil and for the EO conversion respectively.

The sensitivity and the linearity of this conversion has been also studied over the 74 dB range of available power. The result is shown on figure 6. The dynamics exceeds 60 dB and is down limited by the noise floor (\(-112 \text{ dBm}\)) of the spectrum analyser, which is much greater than the \(RIN\) of the laser and the shot-noise on the photodiode (\(-140 \text{ dBm} \) and \(-151 \text{ dBm} \) in a 1 Hz analysis bandwidth respectively). The measurements are also compared with two curves. The linear fitting curve (gray dashed line on figure 6) is written:

\[
P_{out,dBm} = A P_{in,dBm} + k_{conv}. \tag{9}
\]

\( A \) is the linearity factor and is equal to 0.997. \( k_{conv} \) illustrates the conversion factor of the whole transduction scheme. \( k_{conv} = -54.1 \text{ dB} \) is close to \( k_{ant} + k_{EO} \), which is \(-56.7 \pm 0.6 \text{ dB} \). The second equation does not involve any fitting parameter and describes the expected output signal as a function of set-up parameters.

Introducing \( \alpha P = 10^{-5 \frac{\text{B}_{\text{max}}}{10}} \frac{R_{ph} R_{load}}{R_{ph} R_{load}} \alpha \left( \frac{K_{EO} L_{in} L_{out}}{\alpha_{in} \alpha_{out}} \right) \frac{1}{\alpha_{in} \alpha_{out}} = 1.2 \times 10^{-6} \), the expression between \( P_{in,dBm} \) and the output signal writes:

\[
P_{out,dBm} = 10 \log_{10} \left( 10^{\frac{\text{Noise dBm}}{10}} + \alpha P 10^{\frac{P_{in,dBm}}{10}} \right). \tag{10}
\]

The calculated value of \( \alpha P \) leads to an expected output signal that is fully consistent with the measured one (see inset of figure 6). Using the link between \( P_{in,dBm} \) and \( B_x \), given in equation 6, \( P_{out,dBm} \) can also be written as a function of the magnetic field:

\[
P_{out,dBm} = 10 \log_{10} \left( 10^{-5 \frac{\text{Noise dBm}}{10}} + a_B B_x^2 \right) \tag{11}
\]

with \( a_B = 10^3 R_{em} \left( \frac{2}{\mu_0} \right) ^2 \alpha P = 5.9 \times 10^7 \text{ mW.T}^{-2} \).

Moreover, the standard deviation between the measurement and the fit given by equation 9 is equal to 2.1 dB for the whole dynamic range and takes a very low value of 0.20 dB for an input signal ranging from \(-26 \text{ dBm} \) to 14 dBm (40 dB dynamic range). Finally, the minimum detectable field, which is defined by the value of the field equalizing the equation 9 and the noise floor value, is \( B_{min} = 176 \text{ pT} \). This latter value reaches 7 pT considering only the laser RIN contribution to the noise, in a 1 Hz analysis bandwidth.

In order to perform an accurate and reliable measurement of the magnetic field, another relevant parameter is the stability of the experiment set-up. This stability of the output signal is mainly determined by the efficiency of the servo-control system that regulates the optical power and the laser temperature. The output signal is measured along 15 minutes for \( P_{in,dBm} = 14 \text{ dBm} \). The result is shown on figure 7(a).

The standard deviation \( \sigma_{EO} \) with respect to the mean signal is deduced for the distribution represented in figure 7(b). We get \( \sigma_{EO} < 0.2 \text{ dB} \).

IV. MAGNETIC FIELD MAPPING

In a more global use of the transduction scheme for magnetic field measurement, we here propose to evaluate the ability of the set-up to perform a near field mapping. As a characterization example of inhomogeneous magnetic field, in orientation and magnitude, we choose an asymmetric
butterfly-shaped loop coil to be the tested device. Moreover, the typical dimensions of the butterfly-shaped loop coil are similar to the endoluminal coil and the field to be measured will be integrated on its whole radiation pattern. The device under test geometry exhibits a vanishing $B_x$ magnetic field at the crossing between the two loops and allows to exploit the available dynamics of the set-up. For this experiment, the referential is the same as indicated on figure 4: the $x$ axes of the two coils are aligned and the endoluminal coil is translated along the $y$ axis (see figure 8(a)). The algebraic value of $B_x$ static magnetic field is firstly 2D mapped thanks to FDTD simulation (quickfield®) for $z = 0$. From this simulation, we define an interesting 1D path (thick arrows on figure 8(a) and 8(b)) for magnetic field mapping in order to make a comparison between measurement and simulation. Both magnetic field distributions are plotted on figure 8(c).

The experimental result exhibits a dynamics of more than 40 dB and is in good agreement with the simulation, especially for the spatial evolution of $B_x$. Nevertheless, the minimum measured value of $-82$ dB, corresponding the crossing location, is much higher than the noise floor. This is explained by the residual magnetic field surrounding the crossing point and still probed by the coil (mainly $B_z$ for $z \neq 0$). This result also demonstrates the immunity of the transducer relatively to the transverse component ($B_y$) of the magnetic field and illustrate the vectorial behaviour of the sensor.

V. CONCLUSION

A LiTaO$_3$ crystal is used together with an endoluminal coil to demonstrate the ability of such transducer to perform a remote and reliable characterization of RF magnetic field at 3T NMR frequency. The whole transducing scheme has been theoretically studied. The in-lab implementation demonstrates a very good agreement with the expected results. The experimental minimum detectable field is weaker than 1 nT. The accuracy of the measured signal is better than 0.5 dB along a 50 dB dynamic range with a rather good stability (deviation lower than 0.2 dB for a 15 minutes temporal window). The previous mentioned performances allow to map one component of the magnetic field and a vectorial selectivity greater than 40 dB is demonstrated. Development of such sensor scheme constitutes a first step towards a fully pigtailed probe. This technique would also benefit from the potential miniaturization of the crystal size ($h_z \simeq 10 \ \mu m$ for an EO...
waveguide), in order to increase the sensitivity (by a factor 400). Furthermore, optical amplifier (+24 dB typically) can be used to increase the optical modulation after polarization treatment to reach lower minimum detectable field, required for actual MRI system, while keeping advantages of passive and remote EO configuration.

REFERENCES


Reina Aydé was born in Lebanon in 1988. She received the M.Sc. degree in physics of Nano Science and Functional Materials from the Lebanese University Faculty of Science II, Beirut, Lebanon, in 2010. She is currently pursuing the Ph.D. degree in electro-optic microsystem for MR endoluminal coil with the CREATIS Laboratory, University of Lyon 1, Lyon, France.

She is working in collaboration with IMEP-LAHC Laboratory, University of Savoie and Kapteos Company.

Gwenaël Gaborit was born in Lens, France, in 1978. He received the M.Sc. degree in microwaves and microelectronics from the University of Lille, Lille, France, in 2002, and the Ph.D. degree in physics from the University of Savoie, Savoie, France, in 2005. Since 2005, he has been an Associate Professor with the IMEP-LAHC Laboratory, since 2006. He is co-founder of the Kapteos Company and is currently the Chief Science Officer. He is involved in THz spectroscopy and plasmonic. His current research interests include developing electro-optic sensors dedicated to ultra wide band and noninvasive electric field measurement.

Pierre Jarige was born in Brive-La-Gaillarde, France, in 1981. He received the Master’s degree in laser, matter and biological media from the University of Paris VI, Paris, France, in 2007. He is currently pursuing the Ph.D. degree with the Grenoble Institute of Technology, Grenoble, France. He is currently with the IMEP-LAHC Laboratory. His current research interests include development of electro-optic sensors devoted to bioelectromagnetism studies, including SAR measurements.

Lionel Duvillaret was born in Thonon-les-bains, France, in 1966. He received the Ph.D. degree in physics from the University of Paris XI, Orsay, France, in 1994.

He was involved in research on electrooptic sampling with the Institute of Fundamental Electronics, Orsay, from 1990 to 1994. From 1993 to 2005, he was an Assistant Professor of physics working on spectroscopy, electrooptic characterization of electric fields, and electromagnetic bandgap materials with the LAHC Laboratory, University of Savoie, Le Bourget-du-Lac, France. Since 2005, he has been a Professor of physics with IMEP-LAHC Laboratory, Grenoble Institute of Technology, Grenoble, France. In November 2009, he has founded Kapteos SAS, Le Bourget-du-Lac, and is currently the Chief Executive Officer. He is the author or co-author of over 125 journal papers and international conference proceedings and is the author of seven patents.

Raphaël Sablong was born in France in 1975. He received the Ph.D. degree in physics from the University of Grenoble, Grenoble, France, in 2001. He was a Post-Doctoral fellow with the Laboratoire de Physique des Lasers, University of Paris XIII, Paris, France, from 2001 to 2002, working on modeling and device of near-infrared reflectance spectroscopy for muscle oximetry. He is currently an Assistant Professor with the University of Lyon, Lyon, France, and a member of the NMR and Optics: Methods and Systems research team from the CNRS 5220, Laboratoire Creatis. His current research interests include photon migration in scattering media, optical instrumentation development for biomedical diagnosis.

Reina Aydé was born in Lebanon in 1988. She received the M.Sc. degree in physics of Nano Science and Functional Materials from the Lebanese University Faculty of Science II, Beirut, Lebanon, in 2010. She is currently pursuing the Ph.D. degree in electro-optic microsystem for MR endoluminal coil with the CREATIS Laboratory, University of Lyon 1, Lyon, France.

She is working in collaboration with IMEP-LAHC Laboratory, University of Savoie and Kapteos Company.
Anne-Laure Perrier was born in France in 1980. She received the M.Sc. degree in optics, optoelectronics, and microwaves from the Institut National Polytechnique de Grenoble, Grenoble, France, in 2003, and the Ph.D. degree from the Laboratory of Microwaves and Characterization, University of Savoie, Savoie, France, in 2006. She has been an Assistant Professor with Claude Bernard University, Lyon, France, since September 2008, where she teaches electronics and signal processing. She continues the research with the Research Center on Medical Imaging. She designs and realizes RF sensors for magnetic resonance imaging applications. Her current research interests include theory, design, and realization of tunable-impedance transformers and tunable power dividers.

Olivier Beuf was born in France in 1970. He received the Ph.D. degree in physics from the University de Lyon, Lyon, France, in 1998. He was a Post-Doctoral fellow with the University of California, San Francisco, from 1998 to 2000, working on advanced methodological MRI developments for musculoskeletal applications. He was a MRI Application Specialist with Siemens Medical Solutions, France. He joined the CNRS 5012 NMR Laboratory in 2000. He is the head of the NMR and Optics: Methods and Systems research team from the CREATIS Laboratory. His current research interests include radio-frequency coils and sequence developments for medical or biological MRI applications both on human and small animals.